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**Publications**  
**of Prof. Asen L. Dontchev**

**RESEARCH MONOGRAPHS**

- [3] Implicit Functions and Solution Mappings. Springer Monographs in Mathematics, Springer 2009 (second edition under preparation) (with R. T. Rockafellar).
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